

(1) Same figure as on homework, see board for colors.

The "blue angles" all have a reference angle of 30 degrees or $\pi/6$ radians. The "green angles" all have a reference angle of 45 degrees or $\pi/4$ radians. The "red angles" all have a reference angle of 60 degrees or $\pi/3$ radians. (ignore the orange here) (12 points)



Write the corresponding number for each of the following angles:



3 points

What are the coordinates of the points at:

- 1) 2)
- 3)

(2) Solve using any of the methods discussed in class.

(10 points)

 $\begin{cases} 2x - y + z = 4\\ x + 3y + 2z = -1\\ 7x + 5z = 11 \end{cases}$

(3) Use <u>Cramer's Rule</u> to solve the following system.	$\begin{cases} x + 3y + z = 2\\ x + y + 2z = 1\\ 2x + 3y + 4z = 3 \end{cases}$	(8 points)
(No credit given for a different method)	-	

(4) Given the following matrices: $\begin{bmatrix} 1 & -2 & 0 & 4 \end{bmatrix}$

(a-d, 2 points each; e,f 4 points each)

$$A = \begin{bmatrix} 8 & 3 \\ -1 & -2 \end{bmatrix} \quad B = \begin{bmatrix} 1 & 2 & 0 & 1 \\ 3 & 1 & -3 & 2 \\ 0 & 5 & 1 & -1 \\ 0 & 2 & 1 & 1 \end{bmatrix} \quad C = \begin{bmatrix} 9 & 3 \\ -4 & 1 \end{bmatrix} \quad D = \begin{bmatrix} -1 & 7 & -1 \\ 3 & -2 & 1 \end{bmatrix}$$

Find the following, if possible. (If not possible, say so.)

(c) BC

(d) det(C)

(e) AD

(f) det (B)

(5) Given
$$A = \begin{bmatrix} 0 & -1 & \frac{1}{2} \\ 3 & -4 & 3 \\ 1 & -2 & 3 \end{bmatrix}$$

(a) Find A⁻¹

(10 points)

(b) Solve the system of equations by writing it as a matrix equation Ax=B and using the inverse of the coefficient matrix (which you found in part a).

$\int -y + \frac{1}{2}z = 7$	
$\begin{cases} 3x - 4y + 3z = 1 \end{cases}$	(3 points)
$\left[\begin{array}{c} x - 2y + 3z \\ \end{array}\right] = 2$	

(6) (a) Convert from DMS (degree, minute seconds)to decimal degrees, show work. $19^{\circ}45'72''$ (8 points)

(b) Convert from decimal degrees to DMS , show work. 42.6°

(c) Convert from radians to degrees: $\frac{7\pi}{9}$

(d) Convert from degrees to radians, exactly (no calculator): 12°

(7) Graph the angle $\theta = 7\pi/12$ in standard position. Give two coterminal angles, one of which is positive and the other negative. Find the reference angle. (8 points)



(8) (For each of the following acute angles, find 4 angles, one in each quadrant, having the given angle as a reference angle. Answer in the units given, exactly. (12 points)

	Q1	Q2	Q3	Q4
23 [°]				
2π/5				
0.2				

(7) Use matrix methods (Gaussian elimination or Gauss Jordan) to solve: (10 points)

-x-2y-z = -32x + y + z = 16x + y + 2z = 9

You must obtain row echelon form or reduced row echelon form. Be sure to label operations performed at each step.